

# ReMoDeL Explained

## An Introduction to ReMoDeL by Example

## **Technical Report**



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## 1. Introduction

This document describes **ReMoDeL v3**, a high-level syntax for defining models and model transformations. It assumes no prior knowledge of Model-Driven Engineering and aims to introduce related concepts such as *models, metamodels* and *model transformations* from first principles, using simple examples. To give some initial context, the field of Model-Driven Engineering is introduced briefly below.

## 1.1 Model-Driven Engineering

Model-Driven Engineering (MDE) is a general strategy in software engineering that seeks to raise the level of abstraction at which we create and manage software systems. In the future, instead of focusing on detailed implementations in specific programming languages, we will create high-level designs using conceptual models that are much closer to the stakeholders' view of their business processes. These models will be checked, maintained and revised by automated tools, which will also generate the eventual software system.

MDE is concerned with any aspect of the design and implementation of software systems that can be represented and managed using models. Reverse-engineering a design from software is one activity. Checking a design for faults and repairing it is another activity. Improving the quality of a design by refactoring is another activity. Translating a design from one representation into another is a further activity. Generating an executable software system from a design is another activity. Each of these activities involves a process known as *Model Transformation* (MT), the conversion of models from one kind to another.

## 1.2 Model-Driven Development

Model-Driven Development (MDD) is the subfield of MDE which focuses specifically on generating executable software systems from high-level abstract designs. There are several perceived benefits. Firstly, the designs are independent of any particular programming language or execution platform, so if the latter change, the investment in the designs is not wasted or lost. Secondly, when the business needs change, it is far easier to update the design models than it is to intervene at the code level. Code is regenerated automatically from the managed designs. It is expected that this will allow Software Engineers to be more productive and more responsive to change requests.

MDD encompasses a range of approaches. Microsoft's *Software Factories* [1] supply a number of code templates and automatic code generators to build product-lines for similar kinds of software product. The Object Management Group (OMG), a consortium of technology providers and consumers, proposes a specific approach called *Model-Driven Architecture* (MDA) [2], based on a set of curated standards, which tool providers may choose to follow. MDA prescribes three levels of abstraction at which models of systems should be developed:

- Computation-Independent Model (CIM) the business requirements model
- Platform-Independent Model (PIM) the logical system design model
- Platform-Specific Model (PSM) the template for implementation

The Eclipse Foundation provides a partial implementation of some of the OMG's standards in the *Eclipse Modelling Framework* (EMF) [3], which supports the creation of visual and textual editors for models. A number of earlier projects in MDD, such as ATL, Epsilon and

Agile UML are now embedded within EMF. Other independent approaches, such as ReMoDeL [4], are not so strongly tied to MDA.

## 1.3 ReMoDeL History

*ReMoDeL* is an acronym for *Reusable Model Design Language*, reflecting the original goal to specify an overlapping set of languages to model different aspects of software systems [4]. Some were closer to implementation (imperative, functional and object-oriented models) and others closer to design (entity-relationship, business process models).

- *ReMoDeL v1*: specified a set of metamodels, initially focusing on core programming and database concepts. These were published as XML specifications. Model transformations were imperative Java programs that manipulated the XML DOM-tree structures directly, which represented instances of these metamodels.
- *ReMoDeL v2:* specified a set of metamodels as Java packages, whose classes modelled the domain concepts directly, serialised as XML. Model transformations were hybrid declarative/imperative rules, using distinct Java patterns for mapping, merging, updating or splitting kinds of transformation.
- *ReMoDeL v3:* specifies metamodels and model transformations in a bespoke compact syntax, with compilers that convert these into executable Java libraries and programs. Concepts and transformations are expressed declaratively in a pure functional style. Mapping, merging and updating transformations are supported.

This history is provided only for completeness' sake; the rest of this report describes the current version of *ReMoDeL*, which is version 3.

## 1.4 ReMoDeL Today

*ReMoDeL v3* has its own compact syntax for expressing models, metamodels and model transformations. *ReMoDeL v3* syntax is about one third the size of the generated Java code, making it much easier to develop metamodels than in previous versions. This encourages rapid experimentation with different kinds of domain-specific language, since the designer is not burdened with code maintenance.

Designers are free to focus on the constraints captured in particular views of a software system. There may be many such views, expressed in different metamodels. Model-transformation then becomes a layered process of gradual refinement, which exploits the constraints found at different levels of abstraction. A software system should be the result of folding together models that capture the data, time and process views of the system.

## 2. Models and Metamodels

The notions of *models* and *metamodels* may be unfamiliar. A model is any constructed representation of something of interest. A model may capture certain details and ignore others. Informally, a model is a simplified version of the thing being modelled.

In Software Engineering, we are concerned almost exclusively with models of information. This can include models of data, models of processes and models of time. Models must be comprehensible to human Software Engineers, who are involved in the design process. In Model-Driven Engineering, models must also be machine-readable, since programs will transform models of one kind into models of another kind.

#### 2.1 An InTree Model

The easiest way to explain these concepts is through examples. We will use the familiar idea of a tree, which is a well-known data structure in computer science. Figure 1 depicts a model of a tree, as a diagram expressing the structure of the tree model.

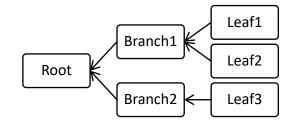


Figure 1: A visual model of an in-tree

The model consists of six labelled nodes, which are connected in a certain pattern. One node is labelled the *Root*, and five other dependent nodes are connected by an arrow to their parent node. Some nodes, labelled *Branch1*, *Branch2*, have further dependents. Other nodes, labelled *Leaf1*, *Leaf2*, *Leaf3*, have no dependents. This model is of a particular kind of tree, called an *in-tree*, in which the root node is reachable from every other node.

```
model tree1 : InTree {
    t1 : Tree(nodes = Node[
        n1 : Node(label = "Root"),
        n2 : Node(label = "Branch1", parent = n1),
        n3 : Node(label = "Branch2", parent = n1),
        n4 : Node(label = "Leaf1", parent = n2),
        n5 : Node(label = "Leaf2", parent = n2),
        n6 : Node(label = "Leaf3", parent = n3)
    ])
}
```

Figure 2: A textual model of an in-tree

The same logical model may be expressed either as a diagram, or as text. Figure 2 depicts the same tree as text, using the *ReMoDeL* model syntax. The keyword *model* introduces the model, which has the name *tree1* and the metamodel-type *InTree*. The model consists of seven typed nodes:

- t1: Tree is a node representing the whole tree, consisting of six nodes
- n1..n6: Node are the other nodes representing the parts of the tree

Each of the nodes has a unique identifier (t1, n1..n6). This allows nodes to refer to each other within the model. For example, the root node has the identifier n1, and the branch nodes n2, n3 refer to this node n1 as their parent. Similarly, the leaf nodes n4, n5 refer to the branch node n2 as their parent. The only node with no parent is the node n1. In this way, the textual notation in figure 2 captures exactly the structure of the tree in figure 1.

Each node has a number of internal properties. Properties can be simple attributes, or references to other nodes. For example, the node n2 has a property called *label*, an attribute which is bound to the simple string value "Branch1". The same node n2 has a property called *parent*, a reference which is bound to the node n1. The bound values of properties are indicated using the simple equals operator.

Some nodes are containers of other nodes. For example, the tree node t1 has a property called *nodes*, which refers to a list of other nodes: *Node[n1 ... n6]*. This makes t1 the container of all the other nodes in the model, and we say that n1..n6 are its components. Containers can be typed either as lists [...], or as sets {...}.

A model is written out as a collection of nodes, having a number of properties. The first time any given node is encountered, it is written out in full, with all of its properties. If the same node is encountered again, only its identifier is written.

## 2.2 The InTree Metamodel

The type of a model is a *metamodel* (a model of a model), which specifies the model's structure and behaviour. The tree of figure 1 is an *instance* of the *InTree* metamodel, depicted in figure 3 using the *ReMoDeL* graphical notation. This specifies what kinds of node are allowed in an *InTree*, and what properties they are expected to have.

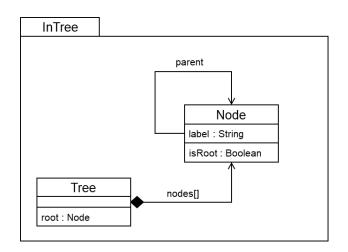


Figure 3: A visual metamodel for InTree

The metamodel is named *InTree*. The metamodel boundary encloses a couple of interlinked concepts, which specify the allowed types of node. These are drawn as rectangles, named *Tree* and *Node*, with two partitions listing their attributes and operations (see below). The references are indicated using labelled arrows drawn from the source to the target. A black diamond at the source-end indicates a stronger component reference.

Readers familiar with the UML notations [5] will notice that the visual syntax bears a certain similarity to UML class and package diagrams. However, the ReMoDeL visual notation is strictly simpler, in that all relationships are directed and are labelled in one direction.

```
metamodel InTree {
    concept Node {
        attribute label : String
        reference parent : Node
        operation isRoot : Boolean {
            parent = null
        }
    }
    concept Tree {
            component nodes : Node[]
            operation root : Node {
                nodes.detect(node | node.isRoot)
        }
    }
}
```

Figure 4: The textual metamodel for InTree

The same metamodel may also be expressed as text. Figure 4 depicts the same metamodel, using the *ReMoDeL* metamodel syntax. This captures all of the information in figure 3, and also specifies the operations. Below, we explain the meanings of certain keywords in the *ReMoDeL* metamodel syntax, drawing analogies with UML and Java:

- **metamodel** defines a given metamodel (c.f. a UML or Java package). All concepts defined within the scope of the named metamodel belong to this namespace.
- **concept** defines a concept within a metamodel (c.f. a UML or Java class). A concept is an entity that may have attributes, references, components and operations.
- **attribute** defines a named property of a concept that stores a simply-typed value. Attributes store *String, Integer, Decimal, Boolean* and other simply-typed values.
- **reference** defines a named property of a concept that refers to another concept elsewhere in the model (c.f. a weak reference, or a directed association in UML).
- **component** defines a named property of a concept that is contained by, and managed locally by, the concept (c.f. an owned reference, or a composition in UML).
- **operation** defines a named operation of a concept (c.f. a method in UML or Java). An operation always returns a result, and may optionally have parameters.

Every concept is named; and every property also declares a type after its name. Types are single, such as *Node*, or multiple, such as *Node[]*, the type of a *Node*-list. A set-type would be signalled as *Node{}*. Operations only require argument parentheses if they accept arguments. The syntax for the body of operations follows a mix of object-oriented and pure functional programming styles, using mapping and filtering:

- *Node.isRoot : Boolean –* returns true if the parent of the node is *null*.
- *Tree.root : Node* filters the list of nodes for the only node that is a root.

The textual syntax is intended to be compiled to generate an executable metamodel, for example, by converting the metamodel into a Java package, and converting each concept into a corresponding Java class definition. The strong versus weak reference model also supports translation into  $C^{++}$ , where memory management is explicit (a class must manage its own components, deleting these when it is deleted).

## 2.3 An OutTree Model

The *in-tree* is only one way in which we could choose to model a tree, in which every node refers to its parent. For example, we might prefer to model the tree as an *out-tree*, in which every node refers to its children. Figure 5 depicts an example of this kind of tree:

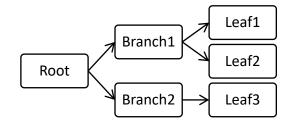


Figure 5: A visual model of an out-tree

The model consists of six labelled tree-nodes, which are connected in precisely the opposite direction to the tree in figure 1. One node labelled *Root* refers to nodes labelled *Branch1*, *Branch2*, where *Branch1* refers to *Leaf1*, *Leaf2* and *Branch2* refers to *Leaf3*. This tree is an *out-tree*, in which every node is reachable from the root.

```
model tree2 : OutTree {
    t1 : Tree(root =
        n1 : Node(label = "Root", children = Node[
            n2 : Node(label = "Branch1", children = Node[
                n4 : Node(label = "Leaf1"),
                n5 : Node(label = "Leaf2")
            ]),
        n3 : Node(label = "Branch2", children = Node[
                n6 : Node(label = "Leaf3")
        ])
        ])
        ])
    }
}
```

Figure 6: A textual model for an out-tree

The same model may be represented either visually, or textually. Figure 6 depicts the same tree from figure 5 as text, using the *ReMoDeL* model syntax. The keyword *model* introduces the model, which has the name *tree2* and the metamodel-type *OutTree*. The model consists of seven typed nodes:

- *t1: Tree* encapsulates the whole tree, whose *root* is bound to the root *Node*.
- *n1..n6: Node* represent other labelled nodes, which refer to their own children.

Contrasting figure 6 with figure 2, there is no single container for all the nodes; instead, *Tree* just refers to the root *Node n1*. Thereafter, each *Node* contains its own *children*. For example, the *Node n2* contains, as its *children*, the list *Node[n4, n5]*. This gives rise to the levels of indentation in figure 6, where nested nodes are introduced further to the right.

## 2.4 The OutTree Metamodel

The different structure of this model is defined by a different metamodel, as you would expect. Figure 7 depicts the *OutTree* metamodel in the ReMoDeL visual notation. This specifies the different allowed linkage between nodes. Overall, the declared *properties* of a

*Tree* in this *OutTree* metamodel are similar to the declared *properties* of a *Tree* in the *InTree* metamodel of figure 3: the difference is in which properties are provided as *components*, and which are provided as *operations*.

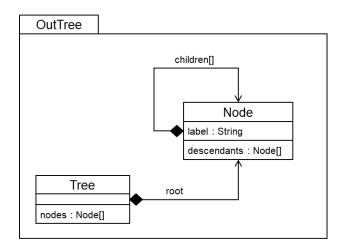


Figure 7: A visual metamodel for OutTree

The metamodel is named *OutTree*, and the boundary encloses two concepts named *Tree* and *Node*. A *Tree* has one *root* component referring to a *Node*. A *Node* has a *children* component referring to a list of *Nodes*. (In the visual notation, the list type indicator [] is added to the label on the arrow, when this refers to a list of the target node. Elsewhere, a list type is indicated by adding this indicator after the type-name: *Node*[]).

The same metamodel is depicted as text, using the ReMoDeL metamodel syntax, in figure 8. The *component* keyword indicates that the *Tree* concept is now a container just for the *root Node*; and that each *Node* is the container for its own *children Nodes*.

```
metamodel OutTree {
   concept Node {
      attribute label : String
      component children : Node[]
      operation descendants : Node[] {
         children.append(children.collate(child |
            child.descendants))
      }
   }
   concept Tree {
      component root : Node
      operation nodes : Node[] {
         root.asList.append(root.descendants)
      }
   }
}
```

Figure 8: A textual metamodel for OutTree

In both metamodels (figures 4, 8), the *Tree* concept defines properties called *root* and *nodes*. Whereas in figure 4 the *nodes* are stored directly, in figure 8 the nodes are computed by an operation which walks through the tree. Likewise, whereas in figure 8 the root is stored directly, in figure 4 the root is computed by an operation which searches the nodes. This illustrates how different design decisions can be made in a metamodel. The featured operations in figure 8 work in the following way:

- *Tree.nodes : Node[]* finds all nodes in the tree in top-down order, by treating the root as a list, and then appending all of the root's descendants to this list.
- *Node.descendants : Node[]* finds the descendants of a node by collating the descendants of each child, found recursively, as a single list.

#### 2.5 A Graph Model

Tree- and graph-like structures can either be modelled using nodes that refer directly to each other, or they can be modelled in a more explicit way, using distinct elements to represent the vertices (nodes) and edges (arcs) in the graph. An example of this is shown in figure 9, in which nodes v1..v6 are *vertices*, and nodes e1..e5 are *edges*.

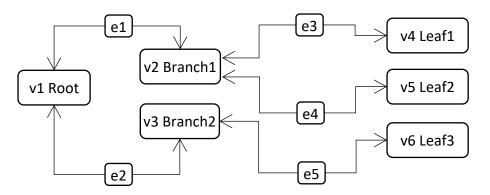


Figure 9: A visual model of a graph

The vertices do not refer directly to each other in this model. Instead, every edge connects a pair of vertices. So, the link from the vertex v1 (the *Root*) to the vertex v2 (*Branch1*) is represented by the edge e1, which refers to the pair of vertices. It is sometimes convenient to build models in this way, because the edges can be added after the vertices, independently.

```
model graph1 : Graph {
   g1 : Graph(vertices = Vertex[
      v1 : Vertex(label = "Root"),
      v2 : Vertex(label = "Branch1"),
      v3 : Vertex(label = "Branch2"),
      v4 : Vertex(label = "Leaf1"),
      v5 : Vertex(label = "Leaf2"),
      v6 : Vertex(label = "Leaf3")
   ], edges = Edge[
      e1 : Edge(source = v2, target = v1),
      e2 : Edge(source = v3, target = v1),
      e3 : Edge(source = v4, target = v2),
      e4 : Edge(source = v5, target = v2),
      e5 : Edge(source = v6, target = v3),
   ])
}
```

Figure 10: A textual model of a graph

The same model is depicted as text using the *ReMoDeL* model syntax in figure 10. From this it is clear that a *Graph* consists of a list of *Vertex[v1..v6]* and a list of *Edge[e1..e5]*.

- *g1: Graph* is a container of lists of *vertices* and *edges*.
- *v1..v6: Vertex* have a *label* attribute bound to a specified *String*.
- *e1..e5: Edge* have a *source* and *target* reference bound to *Vertex* objects.

## 2.6 The Graph Metamodel

The more elaborate structure of a graph model is defined by the *Graph* metamodel, which specifies the relationships between the three types of concept: *Graph, Vertex* and *Edge*. This is depicted in the *ReMoDeL* visual notation in figure 11:

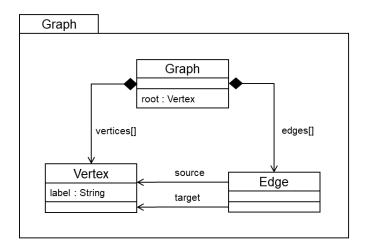


Figure 11: A visual metamodel for Graph

The figure names the metamodel *Graph*, and within the metamodel boundary shows the three concepts. *Graph* consists of a list of *Vertex[]* and a list of *Edge[]*, which are its components. Each *Edge* has two references, one to its *source Vertex* and one to its *target Vertex*.

```
metamodel Graph {
   concept Graph {
      component vertices : Vertex[]
      component edges : Edge[]
      operation root : Vertex {
         vertices.detect(vertex |
            not edges.exists(edge | edge.source = vertex))
      }
   }
   concept Vertex {
      attribute label : String
   }
   concept Edge {
      reference source : Vertex
      reference target : Vertex
   }
}
```

Figure 12: A textual metamodel for Graph

Figure 12 shows the same metamodel as text, using the ReMoDeL metamodel syntax. The *Graph* concept is now the container for every *Vertex* and every *Edge*. Each *Vertex* is merely labelled. Each *Edge* is a separate concept, denoting an arrow from a *source Vertex* to a *target Vertex*. It is possible to find the *root Vertex* by a searching operation:

• *Graph.root : Vertex* – searches for the only *Vertex*, for which no *Edge* exists that has this *Vertex* as its *source* (this is the definition of a root!)

## 3. Model Transformation

The notion of *model transformation* may be unfamiliar. Model transformation (MT) is the process of converting models from one kind into another. In Software Engineering, we are concerned almost exclusively with transformations that affect models representing different views of a software system. Transformations may abstract a design, refine a design, translate a design, or fold together different views of the system.

Model transformations are classified along different, independent dimensions [6, 7]:

- **direction**: transformations are classified as *unidirectional* (they transform a source to a target model), or *bidirectional* if they are reversible (also transform a target to a source model);
- **domain**: transformations are classified as *endogenous* (*rephrasing* within the same language or metamodel) or *exogenous* (*translating* from one language or metamodel to another);
- **valency**: transformations are classified according to the number of source and target models as *mapping* (from one model to another), *merging* (of many models into one), *splitting* (of one model into many), or *updating* (modifying the same model in-place);
- **abstraction**: transformations are classified as *horizontal (migration*, preserving the abstraction-level), or *vertical (refinement*, becoming more concrete; or *abstraction*, becoming more abstract);
- **purpose**: transformations are classified as *translation* (of one model into another), *refactoring* (improving model quality), *enhancement* (inserting features into a model), *normalisation* (simplifying the model), *consistency maintenance* (correction of a model with respect to another).

Model transformations can be expressed as imperative programs that manipulate data structures in an opaque way, or as declarative rule-based languages that express transformations in a more transparent way. Consider the following:

- **Imperative Transformation**: programming language statements may create, modify or delete elements from the model in arbitrary ways. The transformation depends on the states of variables in the program and the order of statement execution, using assignment and iterative loops; and it is not easy to discern the logic being applied.
- **Declarative Transformation**: the transformation is expressed as a mapping from the input space to the output space. The transformation is more like a pure functional programming language (Haskell, ML, etc.) and does not depend on state variables. Repeated actions are accomplished using recursion, and variables are bound just once (not reassigned).
- **Pattern-Matching Transformation**: the transformation is expressed as a logical pattern, specifying a set of constraints between the input space and the output space. Rules are phrased using quantification: "*for all* X in the source, *there exists* Y in the target, such that certain properties hold". This is the most abstract way of specifying a transformation, and must be interpreted, or converted into an operational form before execution.

Clearly, there is a trade-off between the comprehensibility and executability of transformations in these different approaches. Other concerns include:

- *idempotence*, the notion that if the same transformation is invoked in multiple places on the same source entity, it should always yield the same target entity (not a duplicate copy);
- *independence*, the notion that different rules may specify different aspects of the same transformation independently, but these are folded together correctly in the target.

#### 3.1 InTree to OutTree Transformation

The first example model transformation we will consider is a simple *translation*. The *InTree* and *OutTree* metamodels describe *Tree* and *Node* concepts, which support constructing tree models which are broadly similar, apart from the direction in which nodes are linked. It is therefore possible to provide a *mapping* transformation that performs a *horizontal migration* of a model from one metamodel to another (an *exogenous translation*, according to the taxonomy of model transformations).

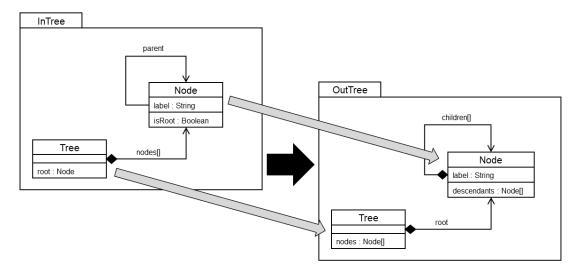


Figure 13: Visualising the InTree to OutTree transformation

Figure 13 illustrates the transformation as a *homomorphism* from one metamodel to another, which consists of a number of *morphisms* that map elements of one metamodel onto elements of the other. That is, the large black arrow denotes the transformation as a whole, which consists of several smaller grey arrows denoting individual rules that map elements from one metamodel onto elements of the other.

Figure 14: The InTree to OutTree transformation

Figure 14 shows the complete model transformation using the *ReMoDeL* textual syntax for transformations. The transformation is called *InTreeToOutTree*, and it belongs to a group of transformations known as *Trees*. It specifies the two metamodels being used (*InTree* for

source entities; and *OutTree* for target entities). It encapsulates a set of mapping rules, which perform the actual transformation. A few more keywords of the *ReMoDeL* syntax are:

- **transform** the keyword introducing a model transformation;
- **metamodel** the keyword introducing source, target metamodels;
- **mapping** the keyword introducing a mapping rule.

All *source* metamodels are declared first, before the *target* metamodel, which always comes last. The mapping rules are declared after this, with the first rule (the *top rule*) being the rule that transforms the topmost element in the model, here *inTree\_Tree*.

A mapping rule may have one or more *source* arguments, and yields one *target* result. The argument and result types are declared in their full metamodel-qualified form, because the type-names alone are not sufficient to distinguish which *Tree* or *Node* we mean (concepts with the same names exist in both metamodels).

Each rule is a function from inputs to output, whose body is a single nested expression in the *ReMoDeL* syntax. The rules have the following meaning:

- *inTreeToOutTree* for each *inTree* : *InTree\_Tree*, create a new *OutTree\_Tree*, whose *root* : *OutTree\_Node* node is the result of mapping the *root* : *InTree\_Node*. This invokes the second rule:
- inNodeToOutNode for each inNode : InTree\_Node, create a new OutTree\_Node, whose label is the same as that of the inNode, and whose children are found by filtering all the nodes of the inTree to select only those child nodes, whose parent refers to this inNode; and then recursively transform this list of InTree\_Node[] nodes into corresponding OutTree\_Node[] children.

To see how the whole model transformation works, imagine that we call the top-rule on the topmost element t1: *Tree* of the *in-tree* in figure 2. This gives the following recursive pattern of rule-invocation, shown in figure 15.

```
t1' := inTreeToOutTree(t1)
  n1' := inNodeToOutNode(n1, t1)
    n2' := inNodeToOutNode(n2, t1)
    n4' := inNodeToOutNode(n4, t1)
    n5' := inNodeToOutNode(n5, t1)
    n3' := inNodeToOutNode(n3, t1)
    n6' := inNodeToOutNode(n6, t1)
```

```
Figure 15: Recursive mapping rule invocation pattern
```

This shows how the elements t1', n1'..n6' of the target model are constructed in turn, by applying the rules to elements t1, n1..n6 of the source model. The indentation in the figure indicates the nested calling of a rule by the next outer rule above it.

The recursion stops, when no further children are found for a given node. For example, the last application to n6 and t1 finds that none of the t1.nodes is a child of n6. Therefore, the *select* method returns an empty list, and the nested *collect* operation likewise returns an empty list, and so the rule is not invoked recursively a further time.

In the body of these rules, we see some examples of the *ReMoDeL* syntax:

- *create* is an operation that constructs a new instance of a concept type. The syntax is: *create Type(property1 := value1, ... propertyN := valueN)*, for as many properties of the type as are supplied (possibly an incomplete list).
- *select* is a filtering operation applied to collections, which retains any object satisfying a test. The syntax is: *collection.select(element | condition-on-element)*.
- *collect* is a transforming operation applied to collections, which maps each element to an element of another type, returning a collection of the same size. The syntax is: *collection.collect(element | transformation-of-element)*.

## 3.2 InTree to Graph Transformation

The second example is a slightly more elaborate translation. The *InTree* and *Graph* metamodels from figures 3 and 11 describe different sets of concepts: {*Tree, Node*} and {*Graph, Vertex, Edge*} respectively. Whereas in the *InTree* metamodel, the nodes refer directly to other nodes, in the *Graph* metamodel, the vertices are connected by explicit edges. Nevertheless, it should be possible provide a *mapping* transformation that performs a *horizontal migration* of a model from one metamodel to another (an *exogenous translation*, according to the taxonomy of model transformations).

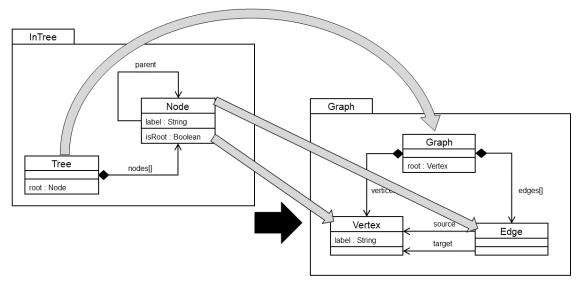


Figure 16: Visualising the InTree to Graph transformation

Figure 16 illustrates this transformation as a different *homomorphism* from one metamodel to another, which consists of a number of *morphisms* that map elements of one metamodel onto elements of the other. The large black arrow denotes the transformation as a whole, which consists of several smaller grey arrows denoting individual rules that map elements from one metamodel onto elements of the other.

The main difference between this and the earlier transformation in figure 13 is the additional rule required. The top rule maps a *Tree* to a *Graph*; another rule maps a *Node* to a *Vertex*; and a further rule maps a *Node* to an *Edge*. How this is done is described more completely in figure 17, which specifies the full details of each rule, using the *ReMoDeL* syntax.

```
transform InTreeToGraph : Trees {
   metamodel source : InTree
   metamodel target : Graph
   mapping inTreeToGraph (inTree : InTree_Tree) : Graph_Graph {
      create Graph Graph (
         vertices := inTree.nodes.collect(node |
            inNodeToVertex(node)),
         edges := inTree.nodes.without(inTree.root)
                     .collect(node | inNodeToEdge(node))
   }
   mapping inNodeToVertex(inNode : InTree Node) : Graph Vertex {
      create Graph Vertex(label := inNode.label)
   }
   mapping inNodeToEdge (inNode : InTree Node) : Graph Edge {
      create Graph Edge(
         source := inNodeToVertex(inNode),
         target := inNodeToVertex(inNode.parent))
      )
   }
}
            Figure 17: The InTree to Graph transformation
```

The transformation is called *InTreeToGraph*, and it belongs to the group of transformations known as *Trees*. It specifies the two metamodels being used (*InTree* for source entities; and *Graph* for target entities). The top rule is called *inTreeToGraph*.

As in the previous example, the mapping rules are functions from input to output, and have the following meaning:

- inTreeToGraph for each inTree : InTree\_Tree, create a new Graph\_Graph, whose vertices : Graph\_Vertex[] are the result of mapping the rule: inNodeToVertex over all the nodes of the inTree; and whose edges: Graph\_Edge[] are the result of mapping the rule: inNodeToEdge over all but one of these nodes, that is, over all the nodes of the inTree except the root node.
- *inNodeToVertex* for each *inNode* : *InTree\_Node*, create a new *Graph\_Vertex*, whose *label* is the same as that of the *inNode*.
- *inNodeToEdge* for each *inNode : InTree\_Node*, create a new *Graph\_Edge*, whose *source* is the result of invoking *inNodeToVertex* on the *inNode*, and whose *target* is the result of invoking *inNodeToVertex* on the *inNode's parent* node.

One aspect of these rules is appealing. Each rule states declaratively how it maps its source to target elements. For example, the rule *inTreeToGraph* states that it uses *inNodeToVertex* to map nodes to vertices, and uses *inNodeToEdge* to map nodes to edges. Similarly, the rule *inNodeToEdge* uses *inNodeToVertex* again, to map the same nodes to source and target vertices. Does this cause problems, if the same nodes are mapped multiple times?

#### 3.3 Idempotence of Rules

To see how applying rules multiple times to some source elements might cause problems, we can trace the pattern of rule-invocation. Imagine that we call the top rule on the topmost

element *t1: Tree* of the *in-tree* in figure 2. This gives the following recursive pattern of rule-invocation, shown in figure 18.

```
g1' := inTreeToGraph(t1)
   v1' := inNodeToVertex(n1)
   v2' := inNodeToVertex(n2)
   v3' := inNodeToVertex(n3)
   v4' := inNodeToVertex(n4)
   v5' := inNodeToVertex(n5)
   v6' := inNodeToVertex(n6)
   e1' := inNodeToEdge(n2)
      v2'' := inNodeToVertex(n2)
     v1'' := inNodeToVertex(n1)
   e2' := inNodeToEdge(n3)
      v3'' := inNodeToVertex(n3)
     v1''' := inNodeToVertex(n1)
   e3' := inNodeToEdge(n4)
      v4'' := inNodeToVertex(n4)
      v2''' := inNodeToVertex(n2)
   e4' := inNodeToEdge(n5)
     v5'' := inNodeToVertex(n5)
     v2'''' := inNodeToVertex(n2)
   e5' := inNodeToEdge(n6)
      v6'' := inNodeToVertex(n6)
      v3''' := inNodeToVertex(n3)
```

#### Figure 18: Recursive mapping rule invocation pattern

Initially, every rule creates a target element (indicated with a single prime x') when invoked for the first time on a source element. However, the rule *inNodeToVertex* is eventually invoked many times on some source elements, mapping to the same target many times, indicated by adding further primes (viz. x'' or x'''). So, for example, the node n2 is mapped to v2 a total of four times:

- firstly, when n2 is mapped to v2' as one of the vertices of Graph g1
- secondly, when n2 is mapped to v2'' as the source of the *Edge e1*
- thirdly, when n2 is mapped to v2''' as the target of the *Edge e2*
- fourthly, when *n2* is mapped to *v2'''* as the target of the *Edge e4*.

From the point of view of writing a declarative specification, this is desirable. It says that: the *Edge* you create for a given *Node*, has a *source*, which is the result of transforming this *Node* to a *Vertex*, and a *target*, which is the result of transforming the *Node's parent* to a *Vertex*.

From a concrete programming point of view, this could lead to a disaster if, every time the rule *inNodeToVertex* were called, this created a new *Vertex*. The resulting model would then contain many duplicates of the same *Vertex*, which is not desirable (and is incorrect).

For this reason, every rule is designed to be *idempotent*, which means that if it is applied more than once to the same *source entity*, this always returns the *same target entity* (and not a new copy of it). The *ReMoDeL* compiler ensures, in the executable code generated for a transformation, that the results of each mapping rule are cached and retrieved, rather than recomputed, when that rule is applied to the same source argument(s) subsequently.

#### 3.4 Inverse Transformations

In some approaches, model transformations are *bidirectional*. This is only possible if sufficient information is preserved in a transformation to support the inverse transformation (if information is lost, this is not possible). Some pattern-matching languages offer rule patterns which can be applied in either direction (forwards, or in reverse). In *ReMoDeL*, transformations are all *unidirectional*, but an *inverse transformation* may exist.

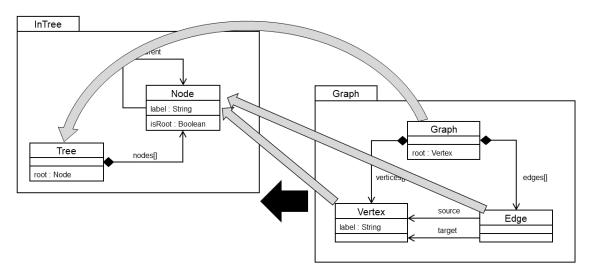


Figure 19: Visualising the GraphToInTree inverse transformation

Figure 19 shows the inverse transformation *GraphToInTree*, which transforms a *Graph* model back to an *InTree* model. This is possible because all of the different representations of trees preserve full information. Figure 20 shows the same transformation in the *ReMoDeL* textual notation:

```
transform GraphToInTree : Trees {
   metamodel source : Graph
   metamodel target : InTree
   mapping graphToInTree(graph : Graph Graph) : InTree Tree {
      create InTree Tree(
         nodes := graph.vertices.collect(vertex |
            vertexToInNode(vertex, graph))
      )
   }
   mapping vertexToInNode(vertex : Graph Vertex,
                          graph : Graph Graph) : InTree Node {
      if vertex = graph.root
         then create InTree Node (label := vertex.label
         )
         else create InTree Node(label := vertex.label,
            parent := vertexToInNode(graph.edges.detect(edge |
               edge.source = vertex).target, graph)
         )
   }
}
```

Figure 20: The inverse Graph to InTree transformation

The transformation rules have the following meanings:

- *graphToInTree* for each *graph: Graph\_Graph*, create a new *InTree\_Tree* whose nodes are the result of mapping the *graph*'s *nodes* using the rule *vertexToInNode*.
- vertexToInNode for each vertex: Graph\_Vertex, create a new InTree\_Node, whose label is the same as that of the vertex; and if the vertex is not the root, whose parent is the result of mapping the parent vertex, using vertexToInNode recursively. The parent vertex is the target of the edge referring to this vertex as its source. The edge is found by searching the graph's edges for the only edge with this vertex as its source.

In the body of these rules, we see some more examples of the *ReMoDeL* syntax:

- *if...then...else* is a conditional expression that tests a Boolean value and then returns the result of either the *then*-branch (in the *true* case), or the *else*-branch (in the *false* case). The two branches return a value of the same type.
- *detect* is a filtering operation applied to collections, which returns a single element passing a test. The syntax is: *collection.detect(element | condition-on-element)*.

In keeping with the pure functional flavour of *ReMoDeL*, the *if...then...else* conditional form is an expression, not a control statement; viz. it returns a value. The *detect()* filtering operation returns an element passing a test, or *null* if none exists. If many elements pass the test, then *detect()* returns the first such element of a *List*, or an arbitrary element of a *Set*.

The transformation *GraphToInTree* makes assumptions about the kind of *graph* to which it is applied. Firstly, it assumes a fully-connected directed acyclic *graph*, with only one *root* vertex. If this were not the case, then the rule *vertexToInNode* would be incorrectly specified. Secondly, it assumes that every *vertex* has at most one parent, such that the graph may be transformed exactly back into a tree.

```
model graph2 : Graph {
   g1 : Graph(vertices = Vertex[
      v1 : Vertex(label = "Root"),
      v2 : Vertex(label = "Branch1"),
      v3 : Vertex(label = "Branch2"),
      v4 : Vertex(label = "Leaf1"),
      v5 : Vertex(label = "Leaf2"),
      v6 : Vertex(label = "Leaf3")
   ], edges = Edge[
      e1 : Edge(source = v2, target = v1),
      e2 : Edge(source = v3, target = v1),
      e3 : Edge(source = v4, target = v2),
      e4 : Edge(source = v5, target = v2),
      e5 : Edge(source = v6, target = v3),
      e6 : Edge(source = v5, target = v3),
      e7 : Edge(source = v6, target = v1)
   ])
}
```

#### Figure 21: A textual model of a directed acyclic graph

What if the graph in question were a more general kind of directed acyclic graph, in which vertices could be linked to many parents and many children? This case is shown in figure 21, in which extra edges e6, e7 have been added to the model from figure 10, to link source vertices v5, v6 respectively to the extra targets v3, v1. This means that v5, v6 have multiple parents.

If we apply the top rule *graphToInTree* to the *graph g1*, the transformation still works (after a fashion), and produces a tree model like that shown in figure 2. The reason that it produces a tree is because the *detect()* operation picks at most one edge to link any given vertex to a parent vertex. In fact, it picks the first such edges found in the model *graph2*, which means that the search never reaches *e6*, *e7*, which are ordered later in the list of *Edges*.

Some information about the graph is lost in this reverse transformation from g1 to t1'. We can see this by applying the forwards transformation *inTreeToGraph* to t1', which yields a graph g1', identical to that shown in figure 10, and not the same as the more general graph in figure 21. That is, the edges e6 and e7 vanish.

From this, we may determine that:

- *InTreeToGraph* has an inverse transformation *GraphToInTree*; viz. it is always possible to convert an *InTree* into a *Graph*, which can be converted back into an identical *InTree*.
- *GraphToInTree* does not have a total inverse transformation; viz. while it is possible to convert a *Graph* to some kind of *InTree*, it is not always possible to convert this back into an identical *Graph*.

## 3.5 Partial Transformations

The rule *vertexToInNode* contains an expression, which depends critically on a graph being fully-connected, with every *vertex* apart from the *root* having a parent. The following is applied to every other vertex, after the *root* has been handled by a special case:

graph.edges.detect(edge | edge.source = vertex).target

That is, the expression assumes that there will always be a detected *edge*, from which it is possible to select the *target* vertex. If no *edge* were found for some *source* vertex, then this code would fail (*null* has no *target*). If graphs are allowed to have multiple roots (a *forest*, rather than a *tree*), this means that transformations to a *tree* will sometimes fail.

This raises the prospect of *partial transformations*, that is, transformations that are not applicable to every source model. The usual way to handle this is to specify a precondition, which accepts only those models to which the transformation may legally be applied.

```
function isTree(graph: Graph_Graph) : Boolean {
   graph.vertices.select(vertex: Graph_Vertex |
      not graph.edges.exists(edge: Graph_Edge |
        edge.source = vertex)).size = 1
}
mapping graphToInTree(graph : Graph_Graph) : InTree_Tree {
    if isTree(graph)
      then create InTree_Tree(
        nodes := graph.vertices.collect(vertex |
           vertexToInNode(vertex, graph))
      )
      else null
}
...
```

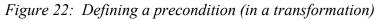


Figure 22 shows how a precondition may be defined as a simple function, which is used in a transformation rule. Functions are distinguished from rules by the keyword:

• function – the keyword introducing an auxiliary function.

Functions are not idempotent, so compute their results every time they are called. Here, the function *isTree(Graph)* is a Boolean-valued predicate which can be invoked on a graph to see if it is in fact a tree (rather than a forest). The body of the function counts the number of roots in the *graph*, expecting this to be exactly one. The roots are found by selecting all vertices in the *graph* with no outgoing edges.

This precondition is tested inside the rule *graphToInTree*. If the precondition is *true*, the transformation may safely proceed; otherwise, it does not exist, and the result is therefore *null*. This is formally correct, if we wish to assert that there is no possible transformation from a graph to a tree, unless it is a single-rooted graph. Of course, it is dangerous to return *null* values, if other transformations expect non-null values (see below).

In figure 22, we expressed the precondition as part of the transformation. It is also possible to specify constraints as part of the metamodel. Figure 23 shows the alternative style, in which *isTree: Boolean* is an operation of the *Graph* concept:

```
metamodel Graph {
  concept Graph {
      component vertices : Vertex[]
      component edges : Edge[]
      operation roots : Vertex[] {
         vertices.select(vertex |
            not edges.exists(edge | edge.source = vertex))
      }
      operation isTree : Boolean {
         roots.size = 1
      }
   }
   concept Vertex {
      attribute label : String
   }
   concept Edge {
      reference source : Vertex
      reference target : Vertex
   }
}
```

Figure 23: Defining a constraint (in a revised Graph metamodel)

Figure 23 is a revision of the *Graph* metamodel from figure 12. Here, we allow the possibility of multiple *roots* (a graph may now be a forest). However, the transformation back to an equivalent *InTree* is only possible if *isTree* holds.

Figure 24 shows a revised version of the partial transformation from a *Graph* to an *InTree*. Here, we assume that the *Graph* metamodel is as specified in figure 23 (where graphs may be forests). The other changes to the original *GraphToInTree* transformation from figure 20 are that the *isTree* precondition has been added in *graphToInTree*, which now returns a failed result as an empty *InTree* (rather than *null*, which would cause problems when saving), and a *root* node is now detected as a member of the list of *roots*, in *vertexToInNode*:

```
transform GraphToInTree : Trees {
   metamodel source : Graph
   metamodel target : InTree
   mapping graphToInTree(graph : Graph Graph) : InTree Tree {
      if graph.isTree
         then create InTree_Tree(
           nodes := graph.vertices.collect(vertex |
               vertexToInNode(vertex, graph))
         )
         else create InTree Tree()
   }
   mapping vertexToInNode(vertex : Graph Vertex,
                          graph : Graph Graph) : InTree Node {
      if graph.roots.has(vertex)
         then create InTree Node (label := vertex.label
         )
         else create InTree Node(label := vertex.label,
            parent := vertexToInNode(graph.edges.detect(edge |
               edge.source = vertex).target, graph)
         )
   }
}
      Figure 24: The partial inverse Graph to InTree transformation
```

#### 3.6 Other Kinds of Transformations

All the transformations considered so far are *translations* from one metamodel to another. Other kinds of transformation are possible. While we don't have room to give examples of these in this introduction, we can describe the flavour of several other kinds.

**Enhancement** – An example of this might be a transformation that ensures that every *Entity* in an *Entity Relationship Model* (ERM) [8] is identifiable. The source and target metamodel is the same (ERM) and consists of a *Diagram* containing *Entities* and *Relationships*. The *Entities* contain *Attributes*, some of which may have an *id* property set to *true*, to indicate a candidate key.

The transformation is *endogenous*, consisting of a collection of *mapping rules*, with a rule to map each concept to the same concept (with changes included). The rule for entities will check whether the source *Entity* has at least one *Attribute* with id = true; and if not, the transformation will append to the target *Entity's* attributes a surrogate key *Attribute*, whose name is synthesised from the *Entity's* name: *entity.name.asName.concat("ID")*.

**Merging or folding** – An example of this might be a transformation that constructs a procedural call-graph (Proc) from two source models conforming to two metamodels, *Jackson Structured Programming* (JSP) [9] and *Dataflow Diagram* (DFD) [10]. There are three metamodels altogether, the two sources and the target. The JSP model *Diagram* consists of named *Blocks*, each marked as one of *{sequence, selection, iteration}* and optionally having component *Block* children. The DFD model *Diagram* consists of named *Process* nodes with *Dataflow* edges indicating what *Datatype* flows from one *Process* to another.

The transformation is *exogenous*, consisting of a collection of *merging rules*, each of which accepts a pair of concepts from *source1* (JSP) and from *source2* (DFD). The rule for *Procedures* will match up a *Block* and a *Process* having the same *name*, and will construct a *Procedure*, whose *Inputs* are obtained from the *Datatype*(s) on the *Dataflow* arrow(s) targeting the *Process*, and whose *Outputs* are likewise obtained from the *Dataflow* arrows exiting the same *Process*. The call-graph structure will be determined from the *Block* structure. The transformation may also generate named *Variables* within a *Procedure* to store the results of executing one sub-*Procedure*, so that these are available to the next sub-*Procedure*. The conditional expressions governing branching and looping will be taken from the *Blocks* marked as *{selection, iteration}*.

**Normalisation** – An example of this might be a transformation that constructs a normalised *Entity Relationship Model* (ERM) [8] in third normal form, from a pre-normal ERM. The source and target metamodel is the same (ERM) and consists of a *Diagram* containing *Entities* and *Relationships*. Some *Entities* are related by many-to-many *Relationships*; and some are related by one-to-one *Relationships*. The rest are related by many-to-one *Relationships*.

The transformation is *endogenous*, consisting of a set of mapping rules that merge sets of *Entities* connected by one-to-one *Relationships*, and split many-to-many *Relationships* into a pair of many-to-one *Relationships* joined to an intermediate linker *Entity*. The merging rule uses an auxiliary function to compute transitive closures over one-to-one related *Entities*, such that any entity in this set is mapped to the same merged *Entity*. All *Relationships* joined to any one of the closure set are mapped to *Relationships* joined to the merged *Entity*. The mane of the linker *Entity* is synthesized, and the composite key *Attributes* of the linker are created by renaming the key *Attributes* of the many-to-many linked *Entities*.

## 4 The Expression Language

So far we have seen only small examples of the *ReMoDeL* expression language. This is the syntax used to define the body of an *operation*, or the body of a *mapping rule*. The same executable syntax is used for both. The expression language is compact and has the flavour of both object-oriented and pure functional programming styles.

## 4.1 Basic Operations

*ReMoDeL* comes with a number of predefined types and operations, which are added to every metamodel implicitly. The predefined basic types are *Boolean, Integer, Decimal, Character* and *String*. These are all valid operands to the comparison operators. The numerical types, *Integer* and *Decimal*, are valid operands to the arithmetic operators, which include modulo and power operators. The *Boolean* values are valid operands to the logical operators.

- constants: null, false, true
- comparison: =, /=, <, >, <=, >=
- arithmetic: +, -, \*, /, %, ^
- logical: and, or, not
- creation: create Type(f1 := e1, ..., fN := eN)
- conditional: if e1 then e2 else e3

Note that the equality operator is a single equals-sign (not a double-equals sign) and the inequality operator is slash-equals (not exclamation-equals), and these test all basic types and collections *by value*, but other concepts *by reference*. The other comparison operators apply to basic types and collections, performing the relevant ordering test. So, <= applied to sets means subset, whereas applied to strings means lexicographic ordering.

The creation operator is used with an initialisation operator (colon-equals) to initialise the fields of created objects. Multiple initialisations are separated using a comma. Due to the pure functional nature of *ReMoDeL*, this is the only time values are assigned. Note that commas are separators, not terminators.

The conditional expression returns either the left or right branch value. These must be of compatible types (the result type is the *least upper bound* type). No parentheses are needed to surround the test-expression (parentheses are only used to alter the precedence of binary expressions). There is no single-branch conditional.

## 4.2 Concept Operations

Every type in *ReMoDeL* is a concept existing in a classification hierarchy. A concept may declare that it inherits from a parent concept within the same metamodel, in which case it obtains the property declarations of the parent concept, before any properties it defines locally. If no explicit parent is declared, the concept inherits implicitly from *Top*, which is the root concept.

- inheritance: concept C1 inherit C2 { ... }
- conversion: asSet: C{}, asList: C[]

*Top* provides two conversion operations that convert any concept into a list, or set. These are invoked like methods. When invoked on a single concept *C*, they return a singleton set  $C_{i}^{f}$  or singleton list *C*[] containing the concept. When invoked on a collection (list or set), they return another collection of the requested type (conversions to the *same* type trivially return the same instance). Whenever any concept *C* is used in lists or sets, the appropriately derived set  $C_{i}^{f}$  or list *C*[] concept is added to the metamodel automatically.

The *String* concept is basic, so offers the binary comparison operations described above that test the string's state. The *String* concept also provides further predefined operations:

```
• predicates:
```

```
isEmpty: Boolean
startsWith(String): Boolean
endsWith(String): Boolean
contains(String): Boolean
```

#### inspection:

```
length: Boolean
indexOf(Character): Integer
charAt(Integer): Character
```

• combination:

```
concat(String): String
cutstring(Integer): String
substring(Integer, Integer): String
split(String) : String[]
```

• case conversion:

asName: String asType: String asWords: String

These support the manipulation of text. The *String*-appending operation is called *concat()* and the *String*-slicing operations are called *cutstring()* and *substring()*. These operations work as in Java – although *cutstring()* is renamed in ReMoDeL, which does not support overloaded *substring()*. The operation *split()* segments a *String* into a list of *String* tokens around a regex-pattern. The operations *startsWith()*, *endsWith()* and *contains()* test for the presence of substrings, and *isEmpty()* tests for the empty String.

Special case conversion operations convert *String* values between "*Word Case*" (normal space-separated words), "*nameCase*" (concatenated text, used for property names) and "*TypeCase*" (concatenated text, used for type names). All of these operations return new *String* values, and do not modify the original *String*.

## 4.3 Collection Operations

The predefined concepts *List* and *Set* inherit from a common *Collection* concept. These types are parametric in the type of their element. You will never see the plain type names *List*, *Set* directly in the expression language, but only specifically typed versions, such as *Node[]* (the *Node*-List type) or *Integer{}* (the *Integer*-Set type).

Collection specifies a common set of operations, inherited by Set and List:

• predicates:

isEmpty: Boolean

```
has(Element) : Boolean
  count(Element): Integer
inspection:
  size: Integer
combination:
  with(Element): Collection
  without(Element): Collection
```

The operations *with()* and *without()* are the principal way of adding and removing elements singly in the pure functional expression language. All operations affecting collections are *constructive*, that is, they construct a new instance of the same kind of collection (they do not modify the collection). The operation *has()* tests whether an element is present in a collection; and *count()* counts the number of occurrences of an element.

The *Set* and *List* concepts provide distinct operations, in addition to those inherited from *Collection. Sets* contain unique elements (viz. no duplicates) and are ordered by element insertion. The *Set* operations that return *Set* results create a new *Set* value:

```
• combination:
```

•

•

pick : Element union(Set): Set intersection(Set): Set difference(Set): Set

*Lists* may contain duplicate elements and are ordered by element insertion. The *List* operations that return *List* results create a new *List* value:

• combination:

first: Element
rest: List
append(List): List

*Lists* may be used in recursive functions, using *lst.first* and *lst.rest* to select the head element and the tail of the list. *Sets* may also be processed recursively, using *set.pick* to select an element, and *set.without(set.pick)* to give the rest of the set. The *asList()* and *asSet()* operations convert from one to the other, where required, preserving order.

#### 4.4 Higher-Order Operations

Collections play a major part in *ReMoDeL*, since rules frequently involve filtering collections to find a subset to which some other transformation is applied. Collections provide higher-order operations that accept a predicate or function argument (a *lambda expression*), applying this to every element of the collection. These operations fall into four groups:

```
• predicates:
```

•

```
forall(Predicate): Boolean,
    exists(Predicate): Boolean
filtering:
    select(Predicate): Collection,
    reject(Predicate): Collection,
    detect(Predicate): Element
```

• mapping:

```
collect(Function): Collection,
collate(Function): Collection
```

• reducing:

reduce(Reduction): Element

A lambda expression is an anonymous function (or predicate) constructed dynamically. It has the syntactic form: (*variable* | *expression-containing-variable*). The variable denotes one element of the collection, and may be declared with a type, which must be the element-type of the collection (for convenience, the type may be omitted, in which case it is inferred from the type of the collection – see below for a discussion of type inference).

A lambda expression is a *predicate* if the body is a Boolean-valued expression. Otherwise, it is a *function*, returning some other typed value. When the lambda expression is passed as an argument to one of the higher-order collection operations, it is applied to every element of the collection. The meaning of these higher-order operations is as follows:

- *forall* accepts a predicate and returns true if all elements of the collection pass this test. The syntax is: *collection.forall(element | condition-on-element)*.
- *exists* accepts a predicate and returns true if any element of the collection passes this test. The syntax is: *collection.exists(element | condition-on-element)*.
- *detect* accepts a predicate and returns the first object passing this test, or *null* if none is found. The syntax is: *collection.detect(element | condition-on-element)*.
- *select* accepts a predicate and returns a filtered collection, selecting objects that pass this test. The syntax is: *collection.select(element | condition-on-element)*.
- *reject* accepts a predicate and returns a filtered collection, rejecting objects that pass this test. The syntax is: *collection.reject(element | condition-on-element)*.
- *collect* accepts a function, which maps each element to an element of another type, and returns a collection of the same size, containing elements of the other type. The syntax is: *collection.collect(element | transform-element-to-element)*.
- *collate* accepts a function, which maps each element to a collection-of-elements but returns a single flat collection, formed by merging the results. The syntax is: *collection.collate(element | transform-element-to-collection)*.
- *reduce* accepts a reduction (a reducing function of two arguments) which combines all the elements of the collection, returning a single element. The syntax is: *collection.reduce(elem1, elem2 | combine-elem1-and-elem2-to-element)*

The filtering operations typically return a collection of the same *kind* as the collection on which they were invoked. That is, filtering a *List* returns a *List*, and filtering a *Set* returns a *Set*. The element-type of the result is typically the same as that of the collection. However, the *select* and *reject* operations may return a collection of a more specific element type (this involves a runtime type cast). The *detect* operation returns one element (or *null*).

The mapping operations return collections of the same *kind*, but possibly having a different element-type (according to the lambda expression). Mapping over a *List* returns a *List*, and mapping over a *Set* returns a *Set* of the same size as the original collection. With the *collate* operation, the lambda expression is expected to map individual elements to *List* or *Set* results (depending on the kind of the visited collection). The results are then merged either using *append* (for *Lists*) or *union* (for *Sets*).

The reducing operation *reduce* accepts a binary function that combines two elements into one element of the same type (e.g. the sum, or the maximum, of two numbers). If applied to an empty collection, the result is *null*. If applied to a singleton, the result is that element. Otherwise, the result is the accumulated aggregation of all the elements in the collection (mathematically, this is a limited kind of *left-fold* reduction).

The operations *select, reject, detect* and *collect* are used frequently. These are operations that filter, or transform *Sets* or *Lists* of items. Because filtering is common in transformations, we may see a *collect* (or *collate*) operation applied to the result of a previous *select* (or *reject*) operation. This gives rise to nested invocations, in which the collection resulting from one invocation may become the subject of the next invocation.

An example of nesting was shown in figure 14, in the rule *inNodeToOutNode*, where a *select* operation is used to filter the list *inTree.nodes*, and then a *collect* operation is applied to this result to convert every selected *InTree\_Node* node to an *OutTree\_Node*.

## 4.5 Variables

The expression language uses named variables to refer to different entities or values. The variables that are in scope at any time may include the following:

- The *attribute, reference,* or *component* properties of a *Concept* may be used within operations of the *Concept*, or any inheriting *Concept*.
- The formal arguments of any operation or transformation rule may be used within the scope of that operation or rule, which may also refer to properties in the outer scope.
- The lambda variables of any lambda expression may be used within the lambda body, which may also refer to variables in the outer scope.
- The following are special variables: *self* denotes the current concept instance; *super* denotes this in its supertype context; and *owner* denotes a component's (optional) back-reference to its owning container type. If present, *owner* is automatically set when the component is added to its container. The *owner* back-reference is transient and is never serialised in models.

The names of variables must be unique within their scope. An exception to this is that variables may also shadow the names of *ReMoDeL* keywords, such as *attribute* and *reference*, without ambiguity due to the context of usage.

## 4.6 Type Inference

The *ReMoDeL* toolset can perform limited type inference, to determine the types of certain expressions, where these are not given explicitly. For example, in figure 4, the *InTree* metamodel has an operation *root: Node* containing an expression:

```
nodes.detect(node | node.isRoot)
```

in which the type of the lambda variable *node* is not given. In this case, the *ReMoDeL* tools determine the type by *type inference*. A lambda variable iterates over every element of the collection invoking the higher-order operation. Here, the collection is a list: *nodes: Node[]*. The type of one element of the list is therefore inferred to be *Node*. To avoid relying on type inference, it is possible to give explicit types to lambda variables, like this:

nodes.detect(node : Node | node.isRoot)

Type inference is more challenging in transformation rules, where there may be more than one type having the same name, in different metamodels. In figure 14, the *InTreeToOutTree* transformation has a mapping rule *inNodeToOutNode* containing an expression:

inTree.nodes.select(child | child.parent = inNode)

in which the type of the lambda variable *child* is not given. We need to know if this refers to an *InTree\_Node* or an *OutTree\_Node*. In this case, type inference seeks the metamodel-qualified type of the collection. Here, the expression *inTree\_nodes* refers to a component declared in *InTree\_Tree*, having the qualified list type *InTree\_Node[]*, from which we infer that *child* has the element type *InTree\_Node*.

This inference is only possible because the rule's argument (in figure 14) was declared with a metamodel-qualified type: *inTree*: *InTree*\_*Tree* in the first place. If types are not given in their qualified forms, then a semantic error may be raised if the type's owning metamodel cannot be resolved unambiguously.

To avoid relying on type inference, it is possible to give explicit metamodel-qualified types to lambda variables, like this:

inTree.nodes.select(child : InTree\_Node | child.parent = inNode)

#### 4.7 Type Conversion

*ReMoDeL* concepts exist in a classification hierarchy. Variables are polymorphic (typed with a general concept, but may receive objects of more specific types of concept). Sometimes, it may be desired to recover the specific type of an object stored in a general variable. This can be done simply by giving the access operation the more specific result type. This will create a type down-cast at runtime.

```
concept Connective inherit Element {
   reference source : Concept
   reference target : Concept
}
concept Generalisation inherit Connective {
   operation specific : ObjectType { source }
   operation general : ObjectType { target }
}
```

Figure 25: recovering specific types by access operation

In figure 25, a very general kind of edge called *Connective* is defined to link a *source* and *target Concept*. Later, a special kind of *Connective* called *Generalisation* is defined that only ever links two *ObjectTypes*, which we assume are kinds of *Concept*. The *source* and *target* may be referenced through the operations *specific* and *general*, which down-cast the results to the declared result-type *ObjectType*.

References or components may be redeclared with more specific types, in concepts that inherit from the one in which they were first declared. Similarly, operations may be redeclared with more specific result types (argument types may not be changed).

```
concept Property inherit Element {
   attribute name : String
   reference type : Type
}
concept Attribute inherit Property {
   reference type : BasicType
}
```

Figure 26: redefining the declared type of a property

In figure 26, a very general kind of *Property* is defined, having a *name* and referring to a very general *type*. Later, a special kind of *Property* called *Attribute* is defined, whose *type* is redefined as a *BasicType*, which we assume is a kind of *Type*. When accessing the *type* of an *Attribute*, this will be returned as a *BasicType*.

```
concept Property inherit Element {
   attribute name : String
   reference type : Type
   operation isAttribute : Boolean { false }
   operation isReference : Boolean { false }
}
concept Attribute inherit Property {
   reference type : BasicType
   operation isAttribute : Boolean { true}
}
concept Reference inherit Property {
   reference type : ObjectType
   operation isReference : Boolean { true }
}
concept ObjectType inherit Type {
   component properties : Property[]
   operation attributes : Attribute[] {
      properties.select(prop | prop.isAttribute)
   operation references : Reference[] {
      properties.select(prop | prop.isReference)
   }
}
```

Figure 27: filtering for a more specifically typed collection

Collections may in general store elements of heterogeneous types, so long as the type of every stored element is a subtype of the collection's declared element type. In figure 27, *ObjectType* has a general list of *properties* : *Property[]*, which is used to store mixed *Attribute* or *Reference* objects.

Such a collection may later be filtered using the *select()* or *reject()* operation, to obtain a more restricted collection containing elements of a more specific type. An example is the operation *attributes : Attribute[]*, which filters the *properties*, returning only those which are in fact attributes, and the result type is *Attribute[]*. Both *select()* and *reject()* may return a more specifically typed collection (types are down-cast at runtime and checked). This is the only kind of type down-casting that may be performed on collections.

## 4.8 Default Initialisation

When creating a new instance of a concept, many of its properties (attributes, references, components) are initialised explicitly. However, if a given property is not initialised in a creation expression, it will be initialised to a default value. This is to allow rules to choose how many properties they wish initialise explicitly.

All of the basic types and collections have automatic default values, which are used if no other initial value is specified:

- *Boolean* attributes are initialised to *false*;
- *Integer* and *Decimal* attributes are initialised to zero;
- *String* attributes are initialised to the *empty string*;
- *List* components are initialised to the *empty list*.
- Set components are initialised to the *empty set*.

This helps to avoid many problems with *null* values, for example, *Strings*, *Lists* and *Sets* can be assumed to exist, even if they were not created explicitly. References to other kinds of concept are initialised to *null*, the empty reference.

Properties with default values are also treated specially when saving a model. When a model is saved (as a *.mod* text file), only those properties that were explicitly initialised are written out. This avoids writing more verbose files with empty flag or counter attributes.

## 4.9 Further Reading

Some of the above tutorial material is summarised in an introductory conference paper about the *ReMoDeL* language and toolkit [11]. This also gives an account of:

- the pure functional semantics of transformations;
- the directed acyclic graph structure of models;

There is a companion report to this one, describing the compilation of *ReMoDeL* to Java [12]. This explains in detail how *ReMoDeL* expressions are mapped to (more verbose) Java language expressions.

There is a two-part report, covering a larger case study in *ReMoDeL* that describes how to convert a UML Class Diagram all the way into a normalised relational database and generate code for this in SQL [13, 14].

The *ReMoDeL* website [4] contains information on how to get hold of the software, how to install an example project, and how to use the *ReMoDeL* tools. All of the other articles about *ReMoDeL* are reachable from the website.

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